

Trabajo grupal de límites

$$1. \lim_{n \rightarrow \infty} \left(\frac{2n^2 + 6n^2 + 3}{3n^2 + 5n - 1} \right)$$

$$\lim_{n \rightarrow \infty} \left(\frac{\frac{2n^2}{n^2} + \frac{6n^2}{n^2} + \frac{3}{n^2}}{\frac{3n^2}{n^2} + \frac{5n}{n^2} - \frac{1}{n^2}} \right)$$

$$\frac{2 + \frac{6n}{n} + \frac{3}{n^2}}{\frac{3+5}{n^2} - \frac{1}{n^2}} = \frac{2}{3}$$

$$4) \lim_{x \rightarrow \infty} \left[\frac{(2x+1)^4 + (3x^2-1)^2 + 2}{(x^4+1) + (x+2)^4} \right]$$

$$\lim_{x \rightarrow \infty} \left[\frac{\frac{(2x+1)^4}{x^4} + \frac{(3x^2-1)^2}{x^4} + \frac{2}{x}}{\frac{(x^4+1)}{x^4} + \frac{(x+2)^4}{x^4}} \right]$$

$$\frac{\left(\frac{2x+1}{x}\right)^4 + \frac{(3x^2-1)^2}{x^4}}{\frac{x^4}{x^4} + \frac{1}{x^4} + \left(\frac{x+2}{x}\right)^4}$$

$$\frac{\left(\frac{2x}{x} + \frac{1}{x}\right)^4 + \frac{(3x^2-1)^2}{x^4}}{1 + \left(\frac{x}{x} + \frac{2}{x}\right)^4}$$

$$\frac{2^4 + \left(\frac{3x^2-1}{x^2}\right)^2}{2}$$

$$\frac{16 + \left(\frac{3x^2}{x^2} - \frac{1}{x^2}\right)^2}{2}$$

$$\frac{16+9}{2} = \frac{25}{2}$$

1, 4, 5 | Diapo 15, Diapo 16

$$5) \lim_{x \rightarrow \infty} \left[\frac{\sqrt[3]{8x^3+1} - 1}{\sqrt[4]{16x^4-2} + 3} \right]$$

$$\lim_{x \rightarrow \infty} \frac{\sqrt[3]{8x^3+1} - 1}{\sqrt[4]{16x^4-2} + 3}$$

$$\lim_{x \rightarrow \infty} \frac{\frac{\sqrt[3]{8x^3+1}}{\sqrt[3]{x^3}} - \frac{1}{\sqrt[3]{x^3}}}{\frac{\sqrt[4]{16x^4-2}}{\sqrt[4]{x^4}} + \frac{3}{\sqrt[4]{x^4}}}$$

$$\frac{\sqrt[3]{8/3+1/x^3}}{\sqrt[4]{16/x^4+1/x^4}}$$

$$\frac{\sqrt[3]{8} / \sqrt[4]{16}}$$

$$2/2$$

$$\boxed{1}$$

Diapo 16 :

$$1) \lim_{a \rightarrow \infty} \left(1 + 1/a \right)^{2a}$$

$$\left(1 + 2/2a \right)^{2a}$$

$$\boxed{e^2}$$

$$2) \lim_{a \rightarrow \infty} \left(1 + 1/a - 1 \right)^{(a-1)}$$

$$\boxed{e}$$

$$3) \lim_{a \rightarrow \infty} (1 + 3/x)^x$$

$$(1 + \frac{1/x}{3})^{x/3 \cdot 3}$$

$$((1 + \frac{1/x}{3})^{x/3})^3$$

$$e^3$$

$$4) \lim_{a \rightarrow \infty} (1 + 2/x)^{5x}$$

$$(1 + \frac{1/x}{2})^{x/2 \cdot 2 \cdot 5}$$

$$((1 + \frac{1/x}{2})^{x/2})^{10}$$

$$e^{10}$$